

Design Invariance in the Classic Consumer Choice Problem

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Design Invariance

- Recovered preferences (or heuristics) should be independent of the elicitation method.
- The experimental setting may affect choices:
 - Framing effects (Tversky and Kahneman (1981)).
 - The risk elicitation puzzle (e.g. Crosetto and Filippin (2016), Pedroni et al. (2017), Zhou and Hey (2018)).
 - Tables vs. formulas (Rubinstein (2006)).
 - Time preferences: textual budgets lines vs. MPLs (Chakraborty et al. (2017)).

Choices from Linear Budget Sets

- Choice from a linear budget set is fundamental in Economics.
- Samuelson (1938), Afriat (1967) and Varian (1982) provide a formal non-parametric theory of revealed preferences in this context.
- Laboratory experiments where subjects are asked to make choices from multiple budget sets, provide relatively large individual level data sets natural for the application of the theory of revealed preferences.
- As opposed to most of this literature, this elicitation method is not based on binary comparisons.

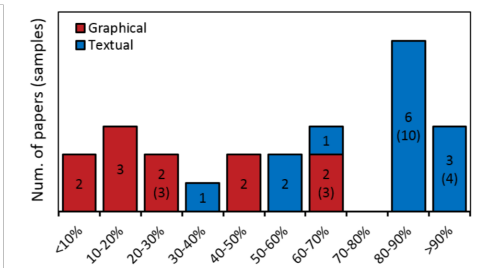
Experimental Designs

- **The Textual methodology** - Subjects are faced with a sentence that describes a budget set and are asked to plug in their preferred bundle.
- **The Graphical methodology** - Subjects are required to choose their preferred bundle from a visually presented budget set.
- These methodologies are used to investigate:
 - Preferences over goods (bundles of various food items).
 - Risk preferences (bundles of Arrow securities).
 - Other-regarding preferences (bundles of Dictator game outcomes).
 - Time preferences (bundles of payments at different dates).
- Other methodologies:
 - Discrete - Subjects are asked to choose among a small number of bundles on the same budget line.
 - Slider.

Contradicting Experimental Evidence (Giving)

	<i>Trials</i>	<i>Price Ratios</i>	<i>No. of subjects</i>	<i>% of GARP satisfiers</i>	<i>Average Afriat index</i>
<i>Fisman, Kariv and Markovits (AER 2007)*</i>	50	Unbounded	76	10.5%	0.108
<i>Andreoni and Miller (ECMT 2002)</i>	8 (8 or 11)	T=3 (T=4)	142 (176)	90.8% (89.8%)	0.003 (0.002)

(*) only two-person treatment.



General

- Two-by-two design.
- One dimension: The context - Dictator (MDG) vs. Risk (RISK).
- Second dimension: The format - Textual interface (Andreoni and Miller (2002)) vs. graphical interface (Fisman et al. (2007)).
- A between subjects design.

MDG: The Setting

- Choices from linear budget sets in the context of other regarding preferences.
- In each decision problem the subject encounters a “modified” dictator game with an anonymous other subject.
- Each token that she allocates to herself is multiplied by α points while a token she allocates to the other is worth β points.

MDG: Textual Interface

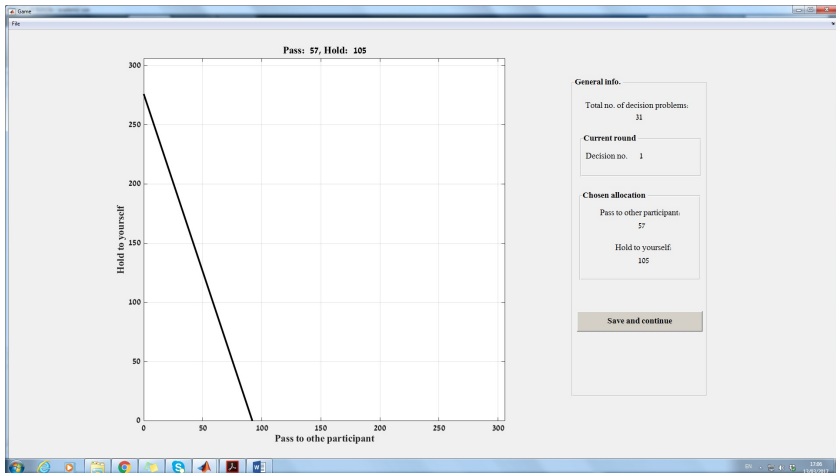
Divide 68 tokens.

Hold tokens at 1 point each.

Pass to the other participant _____ tokens at 3 points each.

Decision problem no. 7 of 41

MDG: Graphical Interface



RISK: The Setting

- Choices from linear budget sets in the context of risk preferences.
- Subjects were asked to choose the optimal portfolio of Arrow securities (two equally probable states) from linear budget sets with varying prices (following Choi et al. (2007b)).
- Each token that she allocates to X returns α points if X is the state of the world while a token she allocates to Y returns β points if Y is the state of the world.

RISK: Textual Interface

Divide 86 tokens.

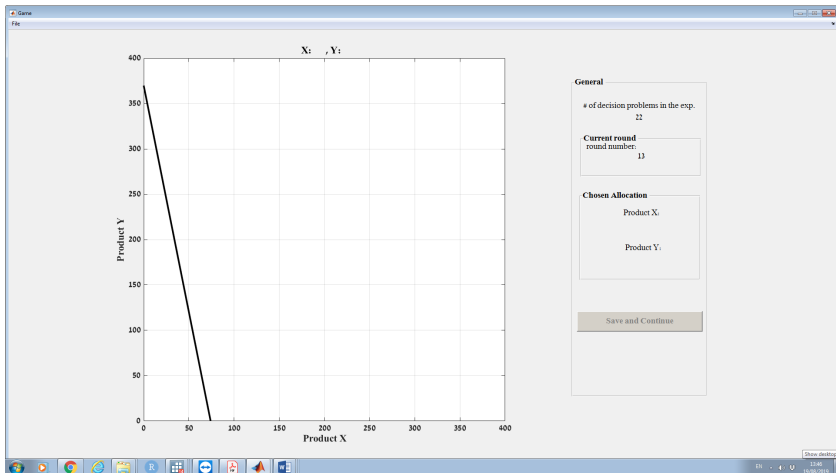
Allocate tokens to product X,
at 1 points each.

Allocate _____ tokens to product Y,
at 3 points each.

Decision problem #9

out of 48

RISK: Graphical Interface

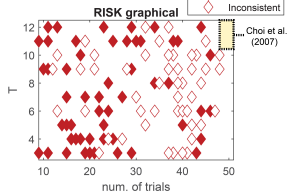
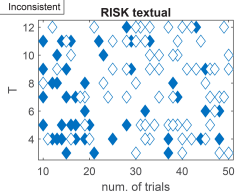
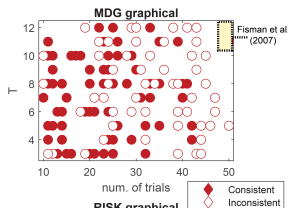
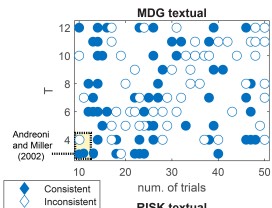


Implementation

- At the beginning of the experiment each subject was randomly assigned with:
 - A number of repetitions (integer between 10 and 50).
 - An upper bound on the price ratio T (integer between 3 and 12).
- In each trial the subject was randomly assigned with:
 - Price ratio (in $\{\frac{1}{T}, \frac{1}{T-1}, \dots, 1, \dots, T-1, T\}$).
 - Tokens endowment (integer between 40 and 100).
- Monotonicity was imposed.
- The subjects were undergrads from TAU and BGU (272 for the MDG and 245 for the RISK).
- The experiments took place in 2016-2017.

Replication

Context	Sample	Num. of trials	Price ratios (T)	Num. of subjects	% GARP satisfiers	Average CCEI
MDG	Andreoni and Miller (2002)	8 (8 or 11)	$T = 3$ ($T = 4$)	142 (176)	90.8% (89.8%)	0.003 (0.002)
	Textual interface	10-29	$T = 3$	10	90%	0
	Fisman et al. (2007) (two person)	50	unbounded	76	10.5%	0.108
	Graphical interface	41-50	$T > 8$	8	12.5%	0.067
RISK	Choi et al. (2007a) ($p = \frac{1}{2}$)	50	unbounded	47	25.5%	0.066
	Graphical interface	41-50	$T > 8$	12	33.3%	



Consistency

Context	Interface	Consistent		GARP violations		CCEI		Varian Index		HMI	
		number	%	all	inconsistent	all	inconsistent	all	inconsistent	all	inconsistent
MDG	Textual	75	55.6%	24.7	55.6	0.047	0.106	0.013	0.029	0.044	0.098
	Graphical	79	57.7%	6.7	15.8	0.027	0.063	0.006	0.014	0.029	0.068
	Total	154	56.6%	15.6	36.1	0.037	0.085	0.009	0.021	0.036	0.083
RISK	Textual	52	41.6%	12.2	20.9	0.034	0.059	0.008	0.013	0.042	0.072
	Graphical	62	51.7%	14.1	29.1	0.032	0.066	0.007	0.015	0.033	0.068
	Total	114	46.5%	13.1	24.6	0.033	0.062	0.007	0.014	0.038	0.070

Result

When the design controls for the number of repetitions and for the range of slopes, the effect of the interface on consistency vanishes and maybe even reverses.

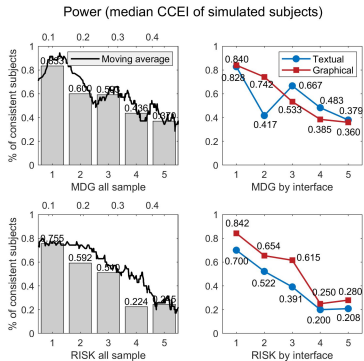
Power: Definition

Definition (Power)

The probability that a DM who chooses randomly uniformly on the budget line will pass the revealed preference test of GARP.

- For each subject, we generated 2,500 simulated DMs.
- Each simulated DM encountered the same sequence of budget sets as the real subject and made random uniform choices.
- For many subjects most simulated DMs failed GARP.
- We opted to use the median CCEI across all simulated subjects as our measure for power.

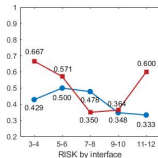
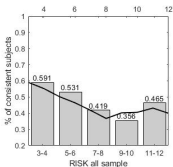
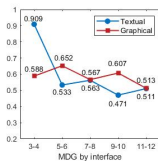
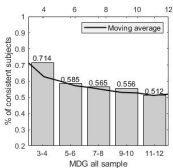
Power: Result



Result

An increase in the power of the experiment leads to a decline in consistency rates, regardless of the interface and the context the subjects encounter.

The Range of Price Ratios



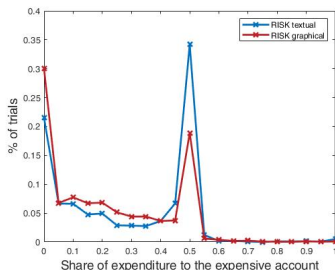
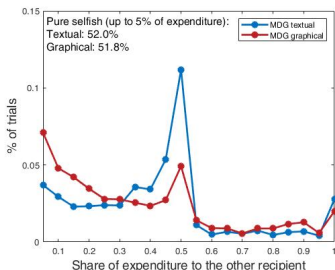
Result

An increase in the maximal slope assigned to the subject leads to heterogeneous effects across contexts and interfaces.

Does the Format Affect Behavior?

- If interfaces differ only in their “user friendliness” then we expect subjects to behave similarly over both interface (after accounting for mistakes).
- Consistency analysis is not adequate to answer this question since it cannot reveal changes in the distribution of behavior.
- Such analysis requires exploring actual choices rather than their internal consistency.

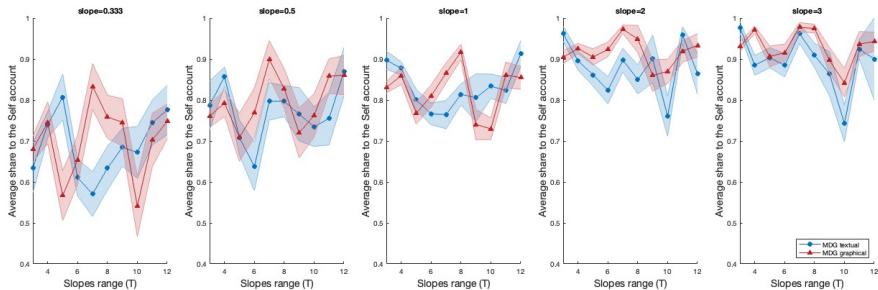
Focal Bundles



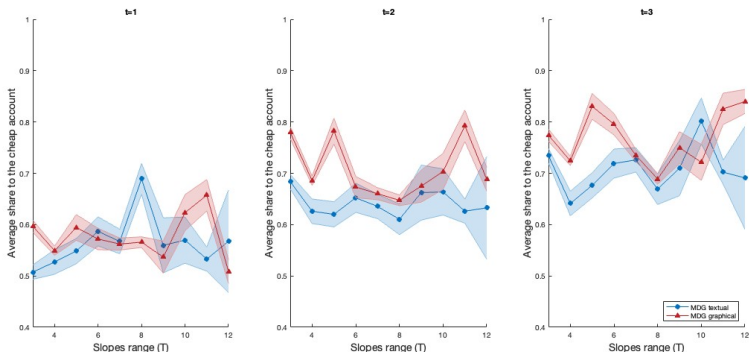
Result

Over all subjects, 50-50 bundles are chosen more in the textual interface. Corner bundles are chosen more in the graphical interface (at least in RISK).

The Range of Price Ratios: MDG



The Range of Price Ratios: RISK



Result

Holding the question and the interface constant, the range of slopes affects, non-linearly, the DM's choices.

Parametric Recovery of Preferences: MDG

In MDG, preferences are usually recovered using the Constant Elasticity of Substitution (CES) utility function

$$u(x, y) = [\alpha \times x^\rho + (1 - \alpha) \times y^\rho]^{\frac{1}{\rho}}$$

where x is the monetary allocation for Self and y is the monetary allocation for Other. $\alpha \in [0, 1]$ is the relative weight on payoff to Self, and $1/(\rho - 1)$ is the elasticity of substitution between Self and Other ($\rho \in (-\infty, 1]$).

- Extreme Altruism: $\alpha = 0$.
- Extreme Selfishness: $\alpha = 1$.
- Egalitarianism: $\rho \rightarrow -\infty$.
- Maximal Social Welfare: $\alpha = 0.5$ and $\rho = 1$.
- Cobb-Douglas with Parameter α : $\rho \rightarrow 0$.

Results: MDG

Type	Definition	Criteria	Methodology	MMI	NLLS
Selfish	$\alpha = 1$	$\alpha > 0.9$	Total	37.1%	56.2%
			Textual	35.5%	60.7%
			Graphical	38.7%	51.8%
Egalitarian	$\rho \rightarrow -\infty$	$\rho < -1$	Total	10.7%	18.0%
			Textual	14.8%	20.7%
			Graphical	6.6%	15.3%
Max Social Welfare	$\alpha = 0.5, \rho = 1$	$0.25 < \alpha < 0.75,$ $0.9 < \rho < 1.1$	Total	1.8%	2.9%
			Textual	2.2%	3.0%
			Graphical	1.5%	3.0%
Altruist	$\alpha = 0$	$\alpha < 0.2$	Total	0%	0%
Unclassified			Total	50.4%	22.8%

- MMI implies NLLS (except 4 selfish-graphical).
- We trust MMI more also due to Halevy et al. (2018).
- Half of the non-selfish subjects are unclassified even in the NLLS.

Parametric Recovery of Preferences: RISK

In RISK, preferences are usually recovered using Gul's Disappointment Aversion utility function (Gul (1991))

$$u(x, y) = \gamma \omega(\max\{x, y\}) + (1 - \gamma) \omega(\min\{x, y\})$$

where x is the amount of Arrow securities type X and y is the amount of Arrow securities type Y. $\gamma = \frac{1}{2+\beta}$ is the weight of the better outcome ($-1 < \beta < \infty$), and ω is a CRRA function with a relative risk aversion parameter ρ :

$$\omega(x) = \begin{cases} \frac{x^{1-\rho}}{1-\rho} & \rho \geq 0 \quad (\rho \neq 1) \\ \ln(x) & \rho = 1 \end{cases}$$

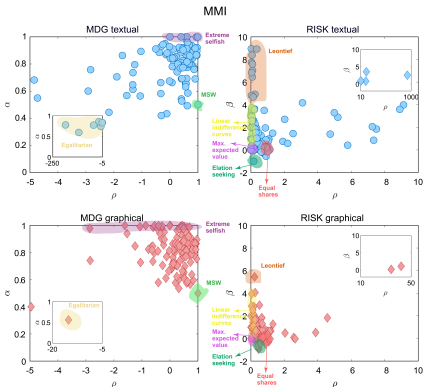
- Expected Value: (i) $\beta = -1$; (ii) $\beta \leq 0$ and $\rho = 0$.
- Cobb-Douglas with Equal Shares: $\beta = 0$ and $\rho = 1$.
- Safe Bundle: $\beta \rightarrow \infty$.
- Switch between safe and corner: $\beta \geq 0$ and $\rho = 0$.

Results: RISK

Type	Definition	Criteria	Methodology	MMI	NLLS
Expected Value	$\beta = -1$ or $\beta \leq 0, \rho = 0$	$\beta < -0.9$ or $\beta \leq 0, \rho \leq 0.2$	Total	9.8%	18.0%
			Textual	7.2%	14.4%
			Graphical	12.5%	21.7%
Safe Bundle	$\beta \rightarrow \infty$	$\beta > 5$	Total	3.7%	8.2%
			Textual	6.4%	12.8%
			Graphical	0.8%	3.3%
Equal Shares of Endowment	$\beta = 0, \rho = 1$	$-0.1 < \beta < 0.1$ $0.9 < \rho < 1.1$	Total	0.8%	5.3%
			Textual	1.6%	4.0%
			Graphical	0%	6.7%
Switch	$\beta > 0, \rho = 0$	$\beta > 0, \rho \leq 0.2$	Total	20%	19.2%
			Textual	24.8%	24%
			Graphical	15%	14.2%
Unclassified			Total	65.7%	49.3%

- Two-thirds of the non-EV subjects are unclassified even in the NLLS.

Summary



Result

The majority of subjects cannot be classified into standard behaviors by parametric elicitation of preferences across contexts and interfaces.

Understanding Behavior

- The most objective way: An algorithm partitions the subjects by their choices and the researcher studies each group's behavior ex-post [We did not do that. Maybe in the future].
- The next objective way: An algorithm classifies each subject to the best fitting predefined choice procedure [We are in the process of doing that (required a list of potential procedures)].
- The non-scientific way: RAs try to “understand” each subject's choice procedure [We have done that].

Choice Procedures

- Informally, a procedure is:
 - A rule for partitioning the observations.
 - A function that assigns a “simple” decision rule to each element of the partition.
- We classified the subjects into a set of procedures.
- Partitions are implemented by cutoffs:
 - Either by price ratio, endowment or observation number.
 - We allow multiple cutoffs.
 - Two cases seem like individual random utility.
- Simple Decision rules:
 - MDG: Give to the other fix or percentage. [For RISK replace “other” with “expensive”].
 - Can work on: Tokens, points or money.
 - On top of that: Rounding (Breitmoser (2021)).
- We include almost all procedures in Halevy and Mayraz (2022) for the case of two firms.

No Cutoff: MDG

Name	Textual	Graphical
Extreme Selfish	41 (30.4%)	34 (24.8%)
Extreme Altruist	0 (0%)	0 (0%)
Egalitarian	13 (9.6%)	1 (0.7%)
Constant Ratio of Money	0 (0%)	2 (1.5%)
Constant Shares of Endowment	6 (4.4%)	6 (4.4%)
Around the Corner	0 (0%)	6 (4.4%)
Nearest Nice Number	10 (7.4%)	1 (0.7%)
Fixed	1 (0.7%)	5 (3.6%)
Total	71 (52.6%)	55 (40.1%)

- In the textual interface more subjects employ simple decision rules.
- 51 subjects (37.7%) in the textual interface and 41 subjects (29.9%) in the graphical interface chose selfishly (using different procedures).
- In the textual interface more subjects implement the egalitarian procedure.

No Cutoff: RISK

Name	Textual	Graphical
Max Expected Value	11 (8.8%)	23 (19.2%)
Safe Bundle	36 (28.8%)	5 (4.2%)
Equal Shares of Endowment	14 (11.2%)	5 (4.2%)
Constant Shares of Endowment	10 (8.0%)	20 (16.7%)
Fixed Insurance	7 (5.6%)	13 (10.8%)
Constant Mix of Safe and Corner	0 (0%)	3 (2.5%)
Total	78 (62.4%)	69 (57.5%)

- Slightly more subjects employ simple decision rules in the textual interface.
- It seems that the subjects faced with the textual interface exhibit more risk aversion than those faced with the graphical interface.

More Complicated Procedures: MDG

- 41 subjects (30.4%) in the textual interface treatment implemented a procedure with one cutoff.
- 39 subjects (28.5%) in the graphical interface treatment implemented a procedure with one cutoff.
- 83% of the textual interface subjects implement one cutoff or less compared to 68.6% of the graphical interface subjects.

More Complicated Procedures: RISK

- 35 subjects (28%) in the textual interface treatment implemented a procedure with one cutoff.
- 31 subjects (25.8%) in the graphical interface treatment implemented a procedure with one cutoff.
- 90.4% of the textual interface subjects implement one cutoff or less compared to 83.3% of the graphical interface subjects.
- Cautious conjecture: Subjects that use the graphical interface tend to use more complicated procedures.

The Classification Algorithm

- For each dataset:
 - The algorithm assigns each procedure with a score (e.g. by its predictive performance, number of hits, revealed preference properties).
 - The algorithm “punishes” procedures for complexity (currently, by number of cutoffs).
 - The algorithm returns the best “simple” procedure.
- Currently, we are calibrating the algorithm - which combination of scoring rule and punishments works “best”.

Things we Learned on External Validity

- A mapping from the design within the lab to “real world” consumer choice problems is necessary but unclear.
- Each design induces different focal choices.
- The design and the variability of problems interact to produce different choices on similar problems.
- Cognitively easier interfaces induce subjects to use more complex choice procedures.

Thanks



Textual Methodology - Hebrew

◀ back

חלקי 60 אסימונים.

שמור/שמרי לעצמך אסימונים
בערך של 1 נקודות לאסימון.

העבר/העבירי למשתתף/ת השניה _____ אסימונים
בערך של 2 נקודות לאסימון.

Textual Methodology - Hebrew

◀ back

דוגמה מספר 1











חלקי/ 60 אימונים.

הקצב/הקציבי אימונים למוצר X,
בערך של 1 נקודות לאימון.

הקצב/הקציבי _____ אימונים למוצר Y,
בערך של 2 נקודות לאימון.

Textual Methodology - Original

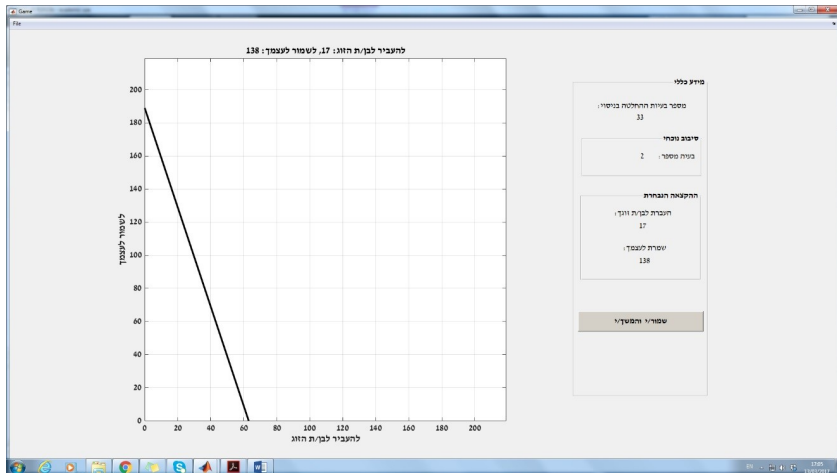
◀ back

	1 other	2 others	3 others	4 others	5 others	9 others			
	Divide tokens with 2 other people						You Earn	Each of 2 others earns	In Total the 2 others earn
1	Divide 45 tokens: Hold 30  @ 20 cents, and Pass 15  @ 30 cents, to each of 2 other people						\$6.00	\$4.50	\$9.00
2	Divide 81 tokens: Hold <input type="text"/>  @ 10 cents, and Pass <input type="text"/>  @ 20 cents, to each of 2 other people								
3	Divide 100 tokens: Hold <input type="text"/>  @ 10 cents, and Pass <input type="text"/>  @ 10 cents, to each of 2 other people								
4	Divide 60 tokens: Hold <input type="text"/>  @ 20 cents, and Pass <input type="text"/>  @ 10 cents, to each of 2 other people								
5	Divide 40 tokens: Hold <input type="text"/>  @ 40 cents, and Pass <input type="text"/>  @ 10 cents, to each of 2 other people								

<-- Clicking this button will submit, at once, ALL of the decisions you made behind EVERY tab.

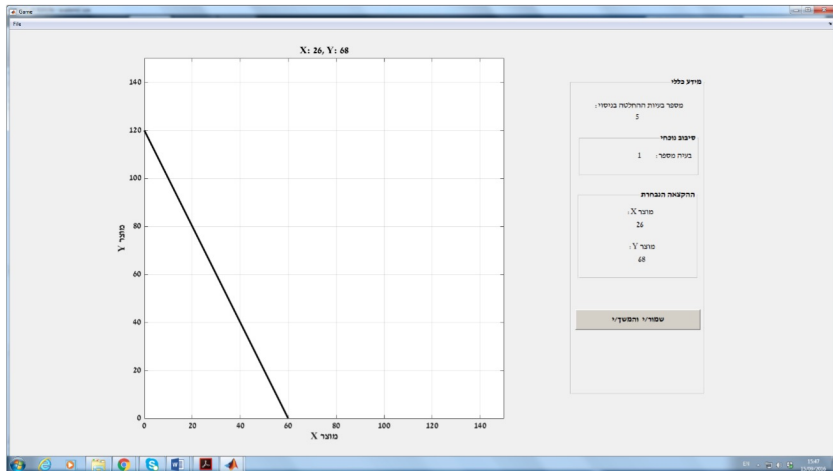
Graphical Methodology - Hebrew

◀ back



Graphical Methodology - Hebrew

◀ back



Graphical Methodology - Original

◀ back

